Can I Switch from doing a Thesis to doing a Project?

Your advisor needs to be on-board with the change. You do not need the approval of the Graduate Director.

Be sure that you have enough courses and ones that fit the categories for doing a project: the key is that you’ll need an additional "breadth" course (thesis requires only 2 breadths and project requires 3).